

Upper Bounds for Equilateral Stick Numbers

Eric J. Rawdon and Robert G. Scharein

ABSTRACT. We use algorithms in the software KnotPlot to compute upper bounds for the equilateral stick numbers of all prime knots through 10 crossings, i.e. the least number of equal length line segments it takes to construct a conformation of each knot type. We find seven knots for which we cannot construct an equilateral conformation with the same number of edges as a minimal non-equilateral conformation, notably the 8_{19} knot.

1. Introduction

Knotting and tangling appear in many physical systems in the natural sciences, e.g. in the replication of DNA. The structures in which such entanglement occurs are typically modeled by polygons, that is finitely many vertices connected by straight line segments. Topologically, the theory of knots using polygons is the same as the theory using smooth curves. However, recent research suggests that a degree of rigidity due to geometric constraints can affect the theory substantially. One could model DNA as a polygon with constraints on the edge lengths, the vertex angles, etc.. It is important to determine the degree to which geometric rigidity affects the knotting of polygons. In this paper, we explore some differences in knotting between non-equilateral and equilateral polygons with few edges.

One elementary knot invariant, the *stick number*, denoted here by $stick(K)$, is the minimal number of edges it takes to construct a knot equivalent to K . Richard Randell first explored the stick number in [Ran88b, Ran88a, Ran94a, Ran94b]. He showed that any knot consisting of 5 or fewer sticks must be unknotted and that $stick(\text{trefoil}) = 6$ and $stick(\text{figure-8}) = 7$. Negami [Neg91] used graph theory to provide the first lower bounds for the stick number in terms of the crossing number, $stick(K) \geq \frac{5 + \sqrt{9 + 8cr(K)}}{2}$.

Several other researchers have provided bounds for the minimal stick number in terms of various knot invariants and have determined the exact stick number for some classes of knots. Using the superbridge index, Jin and Kim [JK93] determined bounds for the stick number of (p, q) torus knots. Jin [Jin97] later extended

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this work, proving that the stick number of a (p, q) torus knot with $2 \leq p < q < 2p$ is exactly $2q$. Working independently, Adams, Brennan, Greilsheimer, and Woo [ABGW97] showed that the stick number of a $(p-1, p)$ torus knot is exactly $2p$. Jin [Jin97] and Adams et al. [ABGW97], independently showed that when one composes two knots, $stick(K_1 \# K_2) \leq stick(K_1) + stick(K_2) - 3$. Citing the limitations in using the superbridge index in bounding the stick number, Furstenberg, Li, and Schneider [FLS98] introduced the radial maximum function and showed that the stick number is bounded below by it. They also determined an upper bound for the stick number of 1, 2, and 3-integer Conway knots. Meissen [Mei97, Mei98] constructed conformations of several knots realizing the stick number by using the knot visualization program KED [Hun]. Concentrating on 2-bridge knots, McCabe [McC98] showed that $stick(K) \leq cr(K) + 3$.

In computing the stick number, one explores the knot space $Geo(n)$ consisting of all polygonal knots with n edges. By choosing a base vertex and an orientation, a polygonal knot can be viewed as a point in \mathbb{R}^{3n} : One simply lists the x , y , and z -coordinates of each vertex beginning at the base vertex and proceeding in the direction determined by the orientation. Thus, $Geo(n)$ can be thought of as a subspace of \mathbb{R}^{3n} . There are no restrictions on the edge lengths of knots in $Geo(n)$ and the edge lengths are free to change in deformations within the space.

Calvo has determined the number of different knot component in $Geo(n)$ for small n . He [Cal98, Cal01a, Cal01b] has shown that there exist five components in $Geo(6)$ consisting of two components each of right and left-handed trefoils and one unknot component. The space $Geo(7)$ has five components, one each for the unknot, left-handed trefoil, and right-handed trefoil and two components of the figure-8 knot. Topologically, the figure-8 knot is reversible, but in $Geo(7)$, it is not. Calvo [Cal01b] also increased the lower bound provided by Negami to $stick(K) \geq \frac{7 + \sqrt{8cr(K) + 1}}{2}$.

The study of other knot spaces has provided interesting results related to the stick number. Cantarella and Johnston [CJ98] studied spaces of knots in which the length of the edges are fixed (and not equal) throughout deformations. They proved that there exist spaces of knots for which the unknot has more than one connected component. Furthermore, knot spaces can be defined for which any knot type has an arbitrary large number of connected components. Thus, the study of polygonal knot spaces has revealed a degree of geometric rigidity not present in the topological knot theory.

Millett and Calvo [Mil94a, Mil94b, Mil01, CM98] have used Monte Carlo explorations of $Geo(n)$ to find conformations of knot with few edges. They provide tables in [CM98] and [Mil01] charting the progress of finding low edge knot conformations of knot types through 9 crossings. Although Monte Carlo searches are interesting in their own right, they have not been effective at finding upper bounds for the stick number of large sets of knots. The data presented in [CM98] showed no improvement over the earlier results in Scharein's thesis [Sch98]. In that work, Scharein found minimal stick candidates for all prime proper knots through 10-crossings (as well as all prime links to 9-crossings) using KnotPlot. Random and deterministic "forces" were applied to the knot to achieve conformations with few edges. We use this large database as a starting point for our exploration of the equilateral stick number.

For some of the knots found in [Sch98], we know that the conformations are truly minimal because of lower bounds determined by other researchers. Other knot conformations are merely *minimal stick candidates*, i.e. no proof is known to show that they are minimal. In these cases, the data provides the *provisional stick number*, denoted by $stick_p(K)$, which is an upper bound on $stick(K)$.

In this paper, we are interested in understanding the minimum number of sticks required to create an *equilateral polygon* of a given type, which we call the *equilateral stick number*, $eqstick(K)$. We use the software KnotPlot [Sch02] to find equilateral conformations for all knots through 10-crossings with a minimal number of edges. Little is known about the equilateral stick number. Certainly, $eqstick(K) \geq stick(K)$, but are there knot types for which $eqstick(K) > stick(K)$ or $eqstick(K) > stick(K) + 1$?

One can also define $Equ(n)$, the subspace of $Geo(n)$ consisting of all equilateral knots with n edges. Here, one need only study the set of polygons based at the origin with total length one to understand the whole space. Any other knot in $Equ(n)$ is related to such a knot by a homothety. Monte Carlo searches in [CM98] suggest that the growth rate of knot types in $Equ(n)$ is slower than the growth rate of knot types $Geo(n)$ as n tends to infinity. If that is the case, then many knots have $eqstick(K) > stick(K)$. However, the different growth rates could simply be an artifact of the Monte Carlo search. Suppose we have a knot type K whose stick number is n . The path component associated with K in $Geo(n)$ is likely to be very small relative to the whole space. The subcomponent associated with equilateral knots of the same type (if it exists) will likely be a tiny portion of the component. Thus, it may be much more difficult to find these small pockets of equilateral conformations of K . Just as for the non-equilateral case, we introduce the *provisional equilateral stick number*, $eqstick_p(K)$, which is an upper bound on $eqstick(K)$. Our computer simulations suggest that the equilateral stick number may in fact be larger than the stick number for some knots, the first such occurrence being the 8_{19} knot. However, we provide no proofs that any of these conformations are minimal.

A topic related to the stick number is the lattice number, that is the minimal number of edges required create a knot on a lattice. This quantity is lattice dependent, but most of the results have assumed the lattice \mathbb{Z}^3 . Diao [Dia93] was the first to find the lattice number for a non-trivial knot. He showed that a non-trivial lattice knot must have at least 24 edges, and that the trefoil is the only knot that can be made of 24 edges. In a subsequent article, [Dia94] Diao exhibited the 3496 unrooted trefoils with 24 edges. Janse van Rensburg and Promislow [JvRP95] used simulated annealing to find low edge lattice conformations through 60 edges. They found 46 different knot types that could be represented with 60 edges or fewer and explored the growth rate in the lattice number for the composition of n copies of a given knot type.

2. Almost Equilateral Knots

Of course, calculating equilateral stick numbers on a computer is problematic: The finite precision of computers takes us from the realm of equilateral knots to “almost equilateral” knots. Working with arbitrary precision can strengthen the case for existence, but a mathematical proof is more attractive. In [Jin97] and [FLS98], conformations of torus knots were constructed using sticks lying on

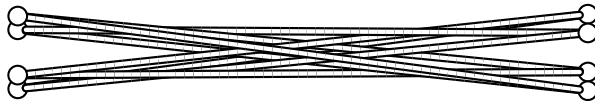


FIGURE 1. Collapse of the 8_{19} knot as it approaches an equilateral state.

hyperbloids (these conformations were not equilateral). One could attempt to construct each of the knots presented here on a surface for which we could explicitly compute the edge lengths. Such constructions, however, are not in the spirit of this paper. We wish to compute equilateral stick numbers quickly without restricting ourselves to certain classes of knots.

Instead, we use a theorem due to Millett and Rawdon [MR01] to insure that equilateral conformations exist near our “almost equilateral” knots. Given a polygonal knot K with an average edge length of exactly 1, let $MD(K)$ be the minimum distance between any two non-consecutive edges of K and let L_i denote the length of the i^{th} edge. If

$$(2.1) \quad |L_i - 1| < \min\{MD(K)/n, MD(K)^2/4\},$$

then an equilateral knot exists with the same knot type as K . The theorem illuminates the delicate balance between the knot being close to equilateral and non-adjacent edges of the knot becoming arbitrarily close. For knots in which it appears that $stick(K) < eqstick(K)$, letting non-consecutive edges become arbitrarily close improves how close we can get to an equilateral knot. During the generation of the data in [MR01], the 8_{19} was identified as the first case for which one had no equilateral knot with the same number of edges as the polygonal knot. Using perturbations to construct an arbitrarily close approximation to an equilateral knot, Millett and Rawdon observed that the closer to equilateral the configuration became, the closer the vertices came to all lying in a plane. This phenomenon is exactly that observed by Calvo in his proof that there is no polygonal 8_{18} with eight edges [?]. As a consequence, this 8_{19} example was proposed as a candidate distinguishing between $eqstick(K)$ and $stick(K)$. Our experiments also suggest that the 8_{19} knot can be made arbitrarily close to an equilateral 8-gon. However, we never obtain a conformation for which the theorem guarantees the existence of an actual equilateral knot. Figure 1 shows what happens with the 8-stick 8_{19} knot as it approaches an equilibrium configuration. The knot appears to “collapse” into 8 nearly colinear line segments. The configuration shown fails the condition in Equation 2.1 by more than a factor of 15.

3. Experimental technique and results

The method used to compute minimal stick candidates in [Sch98] is exceedingly simple. It involves alternating phases of random agitation of the knot and “opportunistic” vertex deletion. Both the random agitation and vertex deletion are done by KnotPlot in a manner that preserves knot type. The initial configuration for the knot is essentially arbitrary; the configurations in KnotPlot’s standard catalogue were used in most cases. For a few knots, a direct construction from the Conway notation for the knot was used instead. Despite this algorithm’s apparent naïvety, the method works very well, usually finding a minimal stick candidate in a few minutes of computer time. Some knots, however, can require much more time

(sometimes many hours) on typical workstations. Examples of “difficult knots” are the knot 7_1 and the torus knots $K_{p,p+1}$ for $p > 5$. For more detail on these techniques, we refer the reader to [Sch98], which also contains many pictures of the minimal stick candidates and representatives.

In this paper, we found equilateral conformations for all prime knots to 10 crossings by starting with the non-equilateral data of [Sch98]. KnotPlot was used to simulate a dynamical system where the vertices of the knot are connected by springs that have a unit rest length. All other of KnotPlot’s usual forces were turned off. Using these dynamics, knots would often move immediately to a nearly equilateral state, but in many cases a phase of random agitation was required before the knot would relax in this way.

Perhaps surprisingly, for 242 of the 249 prime knots¹ to 10 crossings, this method succeeds in finding equilateral versions with the same stick numbers as their non-equilateral counterparts. That is, for these knots $eqstick_p(K) = stick_p(K)$. The seven “problem knots” are 8_{19} , 9_{29} , 10_{16} , 10_{79} , 10_{107} , 10_{119} , and 10_{147} . For each of these knots, we find that $eqstick_p(K) = stick_p(K) + 1$.

Figure 2 shows orthographic projections for three of the equilateral knots found. These knots are shown in a minimal energy conformation for the minimum distance energy E_{MD} [Sim96]. After being brought into an equilateral conformation, all of the knots presented in this paper were relaxed in this manner. For the energy minimization, we used “crankshaft rotations”, popularized by Millett [Mil94b], which preserve edge length. As Simon has shown, energy minimized knots often reveal interesting symmetries when viewed in an orthographic projection along one of the principal axes of inertia. The knots in Figure 2 exhibit this property, but most knots do not reveal their symmetries so easily, as the examples in Figure 3 show (with the exception of the one view of the 9_{47} knot).

Table 1 in the Appendix lists $eqstick_p(K)$ for all prime knots to 10 crossings, as well as the vertex locations for each knot. The numbering is consistent with the Rolfsen table [Rol76], with the exception that the Perko pair has been eliminated. For these knot conformations we find that

$$(3.1) \quad |L_i - 1| < 10^{-2.90} \min\{MD(K)/n, MD(K)^2/4\},$$

so the theorem of [MR01] is satisfied easily, meaning that a true equilateral knot exists for each of these knots. The exponent of -2.90 in Equation 3.1 is for the actual integer data shown in Table 1. This data was rounded to seven significant places in order to reduce the amount of printing space required. If the full 64-bit double precision data is used instead, the exponent is < -11 . The integer data in Table 1 as well as the full precision data is available at the WWW site www.cecm.sfu.ca/~scharein. Also included in Table 2 of the Appendix are the non-equilateral conformations for the seven problem knots.

4. Conclusions

Determining the stick number and equilateral stick number of knots is a difficult problem. If we have found the exact stick numbers and equilateral stick numbers for those in our table, then the results are quite surprising and counterintuitive that $eqstick(K) = stick(K)$ for most K . New theoretical techniques and ideas are needed before we can hope to prove this, however. Unfortunately, most knots (as

¹Not including the unknot and removing one of the Perko pair knots.

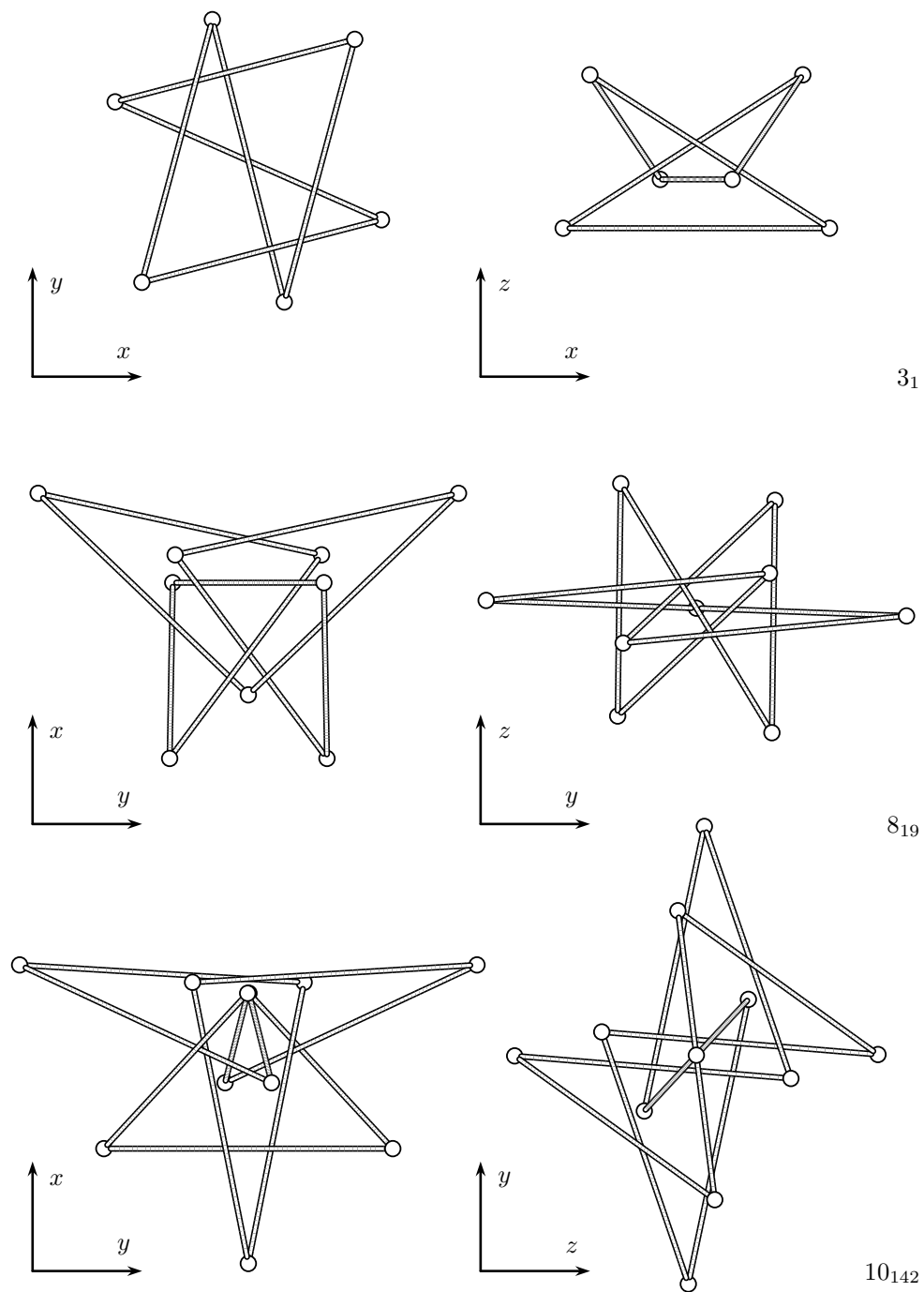


FIGURE 2. Orthographic projections of three equilateral knots along principal axes. All knots have the same edge lengths.

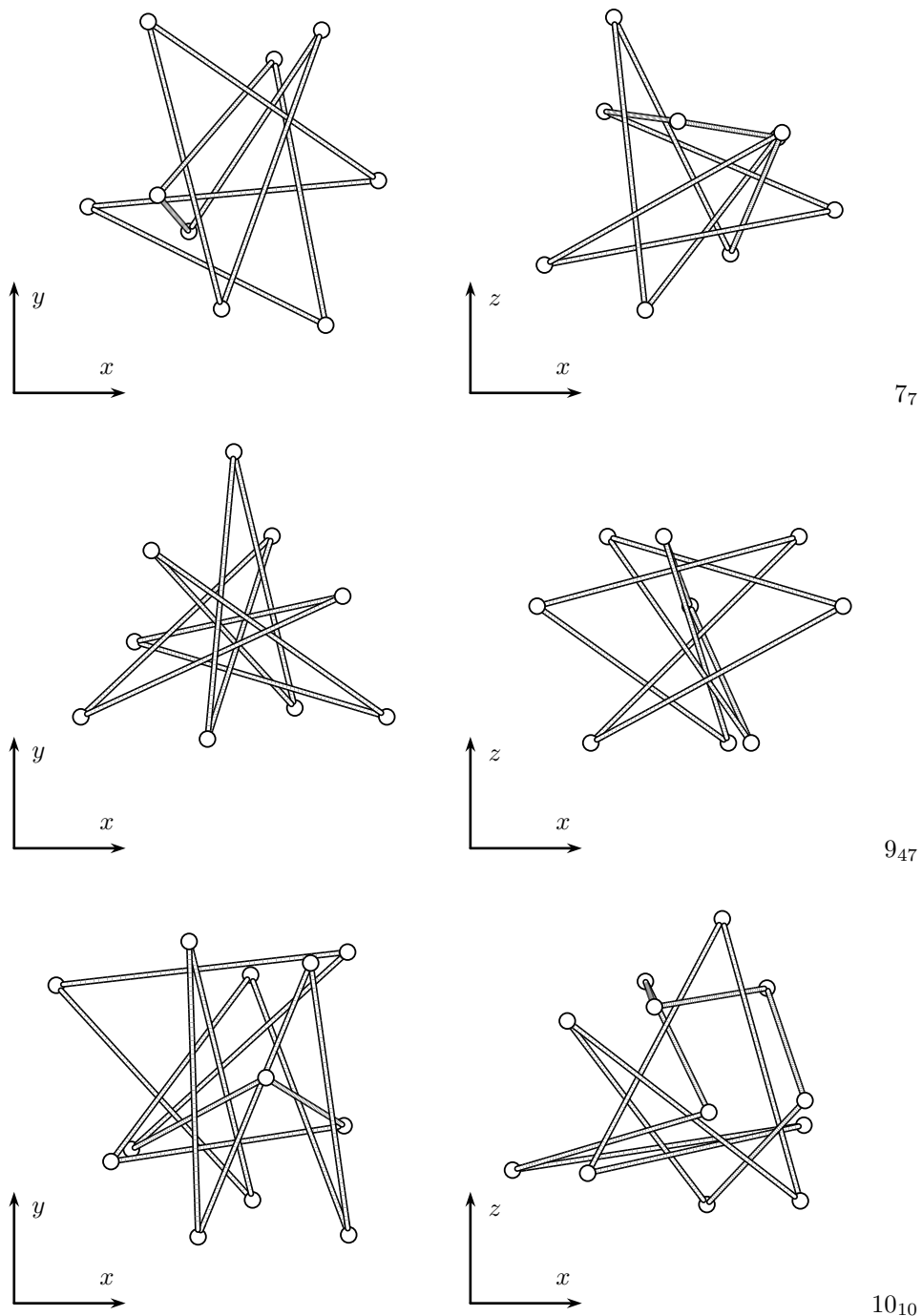


FIGURE 3. Orthographic projections of three more equilateral knots along principal axes. All knots have the same edge lengths.

the crossing number increases) do not appear to have any special characteristics that allow the analysis to be manageable. Successful theoretical studies, e.g. [Jin97, ABGW97, FLS98], have focused on special classes of knots, such as torus knots or connected sums. These knots are exceptional in many ways; the stick number and equilateral stick number of the “average” knot is a more difficult theoretical problem.

The method presented here appears to be quite successful in finding good candidate models for equilateral stick number conformations and identifying candidates for which there may, in fact, be a difference between the stick number and equilateral stick number. The 8-stick version of the 8_{19} knot seems to collapse to 8 nearly colinear line segments as it approaches a nearly equilateral state. However, it seems to never quite reach that state. This provides additional evidence, beyond that in [MR01], that the 8_{19} knot is a very likely candidate for the first knot for which $stick(K) \neq eqstick(K)$. We have developed a tool that can be used in exploring the equilateral stick number for large classes of knots. Some other candidates, one of which might prove to be a more attractive target than the 8_{19} , are also provided in this paper.

Given our results, it is tempting to further conjecture that, in the general case, $eqstick(K) \leq stick(K) + 1$. We feel that this conclusion would be premature. Our results may suffer from the fact that we are considering only the most simple knots and that more complex structures only appear for knots with greater numbers of crossings. As a consequence, it might be that for most knots $stick(K)$ is extremely hard to find, and that the results found in [Sch98] are not the actual values (at least for most of the 9 and 10 crossing knots).

In conclusion, while we know that the equilateral stick number is difficult to determine, this project provides explicit equilateral stick number candidates for prime knots through 10 crossings against which one can test methods for determining the equilateral stick number.

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Appendix

Table 1. Equilateral minimal stick representatives and candidates.
 The first line of each entry indicates the knot type and the provisional equilateral stick number, $eqstick_p(K)$, for that knot. A \star indicates that the value shown is known from theoretical studies to be the actual equilateral stick number $eqstick(K)$.

3_1 1228524 697186 7716595 9718277 2911275 2283329 281723 7088584 2283534 8771546 9302722 7716671 6274418 3 4012316 3725183 9999997 4012154	$6\star$ 6768180 1969142 1648297 3513308 9999997 6428238 1436260 517233 8351703 4881397 7922832 2763789 9255669 3 6767684 744331 4443496 4369945 8507162 9580692 7729161	$7\star$ 9733086 7120748 4806681 233857 6908993 6397009 7898156 1358473 8202444 3887337 6408356 1045534 9766143 9999997 7779707 5793157 2287887 3590664 2042194 9356779 8954466 4215236 3 8221010	5_1 3099634 2243356 8577916 9093861 3335828 2174670 906139 6665496 2192661 6929095 7756620 8569123 6646111 3 4340575 8014739 8230135 1422084 1981556 1770541 1434258 3363877 9999997 4348199	$8\star$ 9469337 3088734 2481786 531233 6911704 2481996 6229952 3 6257945 6333696 9638766 7518214 526668 3098815 3274129 9473332 6901707 3274336 3666696 361200 7518100 3770313 9999997 6258077
6_1 1559033 172965 3967116 5782105 7760718 8008284 7977219 3 2841839 8570648 9373023 4721659 2733394 2261773 7385483 4396684 9999997 1991716 8394961 3197811 7421579 1429352 9571267 5809526	$8\star$ 9733086 7120748 4806681 233857 6908993 6397009 7898156 1358473 8202444 3887337 6408356 1045534 9766143 9999997 7779707 5793157 2287887 3590664 2042194 9356779 8954466 4215236 3 8221010	6_2 9137685 7095816 2350471 3997514 3624162 8299852 3633972 9999997 2547858 1961992 1806556 4533025 7039880 8499288 6347211 7619195 3 5209044 3448813 7325547 6886299 2790538 503570 1700148 862315 8497206 4200671	$8\star$ 9916645 2428244 6805572 1158601 7610103 6913536 5233176 698477 653031 83355 1907376 9346969 4634439 8881522 3497562 5788911 3 8330000 6994424 9999997 6876210 715945 3267266 2538276	7_1 1881019 3 1483399 1964792 7076672 7323993 8275517 1032114 4524552 5821254 9513898 7021496 4179062 486052 7021597 1724483 8967825 4524925 8035524 2923260 7323635 8118614 9999997 1483115 5000242 4999935 8516885
7_2 3 5039425 7556384 9187451 3634633 7053760 3780524 8733632 1450134 9999997 2026495 3172847 6414962 9774439 6881237 5024063 667646 8210520 9411451 8158532 4853033 5134943 225561 2526079 9200251 6041276 8549866	$9\star$ 9137685 7095816 2350471 3997514 3624162 8299852 3633972 9999997 2547858 1961992 1806556 4533025 7039880 8499288 6347211 7619195 3 5209044 3448813 7325547 6886299 2790538 503570 1700148 862315 8497206 4200671	7_3 6992096 3741963 1149787 308547 9999997 4974264 8954169 5130481 4996292 365823 161393 4907359 9691453 1368651 8075101 4804565 9464843 5070199 5794139 462505 1015807 8196792 7722990 7338153 2188010 3 8984193	$9\star$ 1270218 9030689 4655618 1665554 1223692 2225259 4347913 7149270 1795625 7102508 3 4312518 8099032 7801982 2043553 5095611 3003098 7956447 3491629 9999997 4021299 1363142 2160596 4441047 8729782 5661196 4772065	
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8349391 9203443 3187745 6136845 1909135 1434782 9697723 7335211 5799758 6544133 230523 4931747	10 ₁₅ 7944364 5490838 8158487 1982791 6530471 2482965 9936375 4308034 3279213 2062981 1915100 2222670 5150382 9384195 4097055 1508627 1990234 5045577 2656725 9999997 6878144 1534836 1824029 7731171 3370975 7371395 1841513 6272161 3 4306962 63625 5356838 5568363	11 2879414 3650101 1176918 3785999 2392536 8823082 8530205 6207123 3943674 1320141 3486621 2726693 7553022 563671 6397490 3411479 6427780 3343470 8679859 1043644 1313089 6537359 5534811 7321941 1820230 3 4496735 2471646 7488371 6586520 8154015 2432973 4848467 6667206 9999997 3666626	10 ₁₆ 2831073 6299402 7487355 9999997 3344598 4441405 3253481 8218452 4077790 5856110 315040 4483444 3 5984989 2763023 7674060 9160637 3415906 2403423 3285157 6080728 7641100 9684960 7086423 4011519 2239769 7979412 4069119 8764027 2799365 5452655 585917 2020588	12 3179216 1595343 2285012 9999997 2968233 5401728 3638837 4004606 1329459 7098755 9475538 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UPPER BOUNDS FOR EQUILATERAL STICK NUMBERS

10_{37} 12 3243093 1215515 4980153 7576831 6175306 8467220 8146684 3505240 1532780 7893900 9999997 5178968 6533124 3154533 7792081 149892 6191790 5432023 5076092 1305939 8152586 2532255 6908335 3947531 4944813 3 2535101 2811438 4988055 7644749 9850108 4303780 5293293 3956508 8472683 3442296			10_{38} 12 760491 5708823 4426588 5774174 3 4295190 4573260 6854452 1242447 2376776 4129366 7987391 5906378 9612457 4085785 3670591 3142345 786722 8920223 6484396 5147566 3778065 890567 5037139 3412120 8311939 6629063 9239509 4421131 3688307 4107565 9999997 4221511 6598115 4840121 9213278			10_{39} 13 7244183 5115567 7628467 1347419 891772 4137536 3267809 7097474 8891506 4580384 5516099 1108494 586044 3690726 7854762 7286954 807990 4450867 4959863 7610445 8071657 2878052 3 6476006 2934478 7974534 5379405 9413956 3256155 6122461 5078683 9999997 5397986 3944084 2117704 4222824 3559671 9933838 2336255			10_{40} 11 6760811 4196703 1096782 7599877 3 8714478 8258094 6621844 3052007 2932417 835618 6860203 4665633 9231412 5171356 8207211 2011036 1755364 807975 4769301 5495536 8982169 1770353 6226605 6046914 9999997 6173231 4800989 1672585 3839248 9192025 7277994 8903218		
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10_{49} 11 2068771 1512672 4668052 6529915 9392037 7749418 3146575 4141526 5060665 9766516 9999997 4157876 7337931 1371082 822488 233484 7354731 3103670 8903854 3974477 894690 5540281 1480407 9493935 3674896 7436276 2246247 9450431 3 3927335 7264385 9143317 2166079			10_{50} 12 1721351 5298064 1473132 8268690 1019583 4760923 8512270 9314782 2996568 6432567 3024476 8296520 4598217 9999997 3828872 4820993 1521930 4064177 1676838 8745319 7213710 7937011 7974091 1539378 1487730 3200394 4296406 8441260 7859538 5683276 6741424 3 2977564 6304665 6402899 8526868			10_{51} 12 1456315 9999997 6011226 970335 1726051 5844151 9029665 2089108 3936886 1654190 4816515 1312787 7913172 8197612 5569030 7928079 3 4335640 4298994 7295041 2807752 1149598 53296 5329797 8299288 3763363 7289286 3638288 1106959 969408 1744973 1500578 9030592 4162657 3663516 1401780			10_{52} 11 5091496 2346331 9144364 2875488 9548666 5150303 6282513 1785486 4221823 9999997 9308867 5744525 3158501 6136770 1760843 6970152 166244 6510682 6567647 7942860 3032307 3 7391628 8445167 4089372 1537001 3782843 5771854 9833756 4817236 3126049 2759698 855636		
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639313	9655389	7176408	923501	6826473	4456082	9321215	1441075	2562731	4385600	4921697	6213327
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1371803	7826011	4507929	7196464	3	1748357	7910275	8351744	1061531	4673933	6336545	7662976
9360687	6579621	5093520	6696550	8520081	1634400	9773034	3	4336053	9155276	7066811	3231357
4972603	3	3312506	8827575	2201452	6962466	4137126	6727232	1704536	5524206	2649422	5980353
3394487	6002547	8527646	3812290	9087658	6431704	3842760	1112294	8938469	1507536	5942973	2337024
2856647	9654632	1310190	4500684	1187147	3275334	6386751	8461140	4094244	6820824	3137538	4375032
2578864	2166212	4402934	4241326	9708257	2853373	226966	2010714	1998297	6240237	9309257	5726981
4371715	9999997	5468844	1591623	2852580	7193118	3534075	9999997	5027874	844724	5999177	5294795
2745352	2740590	8689810	5966844	9999997	5572473	3208687	1268511	2271206	6831073	7035473	7123645
7661204	7153034	3990512	2443703	2898320	2408885	5801658	7434655	8532125	2956903	2912353	4252120
			9076499	8270467	2382892				8355894	6234711	4512501
									7503861	3	3701685
10 ₆₅	12	10 ₆₆	12	10 ₆₇	11	10 ₆₈	12				
6359193	3	5474004	4683313	3633001	8086953	5880717	1904174	287199	4628054	9999997	7441427
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9234983	4471165	6093473	7525192	2336576	3564669	319711	7193030	2568982	6447241	2792745	7404575
765017	1823964	4886110	2534809	6492498	7006790	8049461	2837077	6235183	3916494	9702266	3427494
7073106	6974709	1160044	8492212	5297669	2870906	5104327	9999997	562163	1014171	2912099	7356041
2468277	7117008	8839956	4010706	3	5294670	820678	3701638	6405571	7417858	4811283	2321213
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10 ₇₃	13	10 ₇₄	12	10 ₇₅	12	10 ₇₆	13				
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10 ₁₂₉ 618059 2596239 4533226 6445146 8774804 1850734 7559894 3 2892645 9381941 8213314 5816178 4393265 2270076 1443946 4014065 9999997 5851884 8246348 2166058 5645593 2647501 7356621 1059054 4572464 3715617 8956078 8423243 5092082 1043922	10 ₁₃₀ 7098802 9999997 8075406 5279194 3 8463487 8036434 7508121 2179600 1843137 742437 6576194 8505691 8281427 5081049 3486542 175511 1536513 987285 9036830 5859961 9012715 2856785 4932064 1784900 9496694 2261527 7620230 1198516 3003572	10 ₁₃₁ 4944919 3 5940307 9896309 5900936 8693185 5044953 1941896 3429541 5703203 9999997 4674256 5720303 3085406 9045038 5991196 4265608 954962 2336458 8571150 6872799 8925323 3891310 5607274 1676000 253795 6670951 7449269 4243401 2467618 103691 6555100 5226991	10 ₁₃₂ 4738755 1490566 5202084 2233240 9999997 5884395 4210015 3102866 623642 3920909 8459243 7721474 6671414 3 7549572 9403117 7343379 3334576 721580 6415934 5044643 8324403 8024317 9376358 596883 4148508 7274667 5418976 9963375 2574847
10 ₁₃₃ 7015528 2422357 1458420 8380353 9073654 5722138 607756 7135782 5385731 6516135 2729711 8541580 5137956 9999997 5455263 8846070 3125942 3644449 1438869 2493385 6646955 9392244 2236424 7626543 5297902 7469347 3139376 2957626 3 4875407 6324191 6362083 8406974	10 ₁₃₄ 9999997 7424780 5158665 3 7820387 5420334 6401527 143435 5976881 3825866 9817669 5980253 7532435 972516 8852441 2149595 2730064 596478 6062208 9856565 6438507 4243230 192081 4563962 8218588 9275271 3179388 1021479 6162935 9403522	10 ₁₃₅ 6111470 8889243 7734695 1435643 2472504 3078592 8980258 7607219 4274706 1083477 3381178 6395702 6169396 9443844 1695202 8397399 2889469 7760956 2578308 9999997 8304798 9064303 4052577 5607159 935697 8365301 5398888 4756952 3 5769017	10 ₁₃₆ 279312 6768598 7047573 7278254 8710328 3350736 7483974 2552912 8686092 9160646 5596231 1313908 4536083 9999997 6377738 5895928 2282224 4139677 9720688 8751097 7293566 2493578 8258989 3558754 9233301 5672476 7341371 4081031 3 4566612
10 ₁₃₇ 6007611 2025972 1948403 5199139 6662608 7535033 8149795 3 7019501 5547919 5927623 3634828 2210727 794689 7619622 6779917 6477853 8051597 2391824 2931262 3411684 2822206 9999997 5203391 3461773 2726207 4990359 8430651 8029436 4249779 1569349 6206965 5971285	10 ₁₃₈ 4818359 9999997 3040077 2840994 2385968 6762369 8023885 7382872 1872845 3752337 3 3600843 4101024 8131629 6682065 1315781 1294160 2074430 7816899 5169250 6370709 1701072 8344872 1055548 8684219 4001928 3903943 2483632 7449370 8944452 8083501 2151554 4905458	10 ₁₃₉ 536313 2111353 8379636 8419054 6971420 7803888 3825401 3 3755797 8332081 8045679 4778678 3992754 1314536 9463901 1992852 9999997 6884655 8064135 3024067 7636499 2897081 6019932 536099 2474943 9666951 9057273 9463687 4025736 6728430	10 ₁₄₀ 6331740 9002545 3034305 1204260 2434165 4537559 9483935 4204514 4622973 3427528 9999997 3428506 4974924 1901963 1499299 8269964 7230103 7195619 6274759 3 3266339 516065 5915612 5147153 7911147 5377618 1058417 6005014 2945173 8941583
10 ₁₄₁ 7141979 3 5079786 1994960 5684202 1400248 6518235 5903412 8599752 5945239 683929 1908743 1273602 4882191 7643839 9144689 4589517 4434282 855311 2998787 3387038 5287999 9999997 5304829 6131063 1776303 7304961 8416437 7655155 1599079	10 ₁₄₂ 7883258 6219992 6138153 1737121 5000194 5000173 7883107 3780008 8861795 8262879 9999997 5175342 5687253 4491730 7068238 7643302 4985372 1027701 4247679 1841416 5402994 4247796 8158741 4597201 7643603 5014714 8972299 5687119 5508364 2931903 8262747 3 4824522	10 ₁₄₃ 8832942 5284225 3249510 5245209 1601285 9999997 3681168 8340786 5086969 5452268 1784039 3 8901831 4567443 7235895 1503865 2484954 3638913 6505485 9102700 5426142 7362991 808044 3855058 8562812 9191956 4379828 7597699 1245394 7195080 1098169 6651071 6460424	10 ₁₄₄ 7024944 8395224 6790552 3 4772070 2354702 8106312 888948 1187263 2599460 5185961 6963426 9999997 9782882 4462593 7041900 1411752 6286775 1918529 8063770 2827257 3320047 1362563 8812737 3866205 9041681 4028738 5718734 217118 3107320
10 ₁₄₅ 248824 1506400 8635906 9751176 4927030 5637355 275197 9422994 4647992 7086879 1656007 6712358 2521789 9714960 1692405 3464826 3 5656870 8311422 9351099 5889734 2495525 1649628 1664879 5487021 9999997 7348979 7870020 1663980 1364094	10 ₁₄₆ 3754161 9427313 5027209 4839259 3 7441652 6467330 6804780 591431 9304044 5664172 9893753 1456375 1191231 6113803 9704069 6403019 5280765 295931 8609783 3700167 6267409 857912 3338095 7307431 9999997 6687988 9296444 3028221 106247	10 ₁₄₇ 2481575 4827742 6945399 6880441 6004103 4830100 3906748 9999997 5461220 4330210 5017621 5913926 4231439 3 6062526 6164511 4468463 7289076 2818708 6884602 4429669 7518425 6763836 6192170 4334216 3841386 3637091 3985812 7755009 6762870 5171107 5037447 2710924	10 ₁₄₈ 542933 3 4676755 4975296 7291843 3458919 4538051 400696 8618454 601356 6330851 3756810 7778227 2100169 5968990 5934530 9999997 3054649 275446 8448979 9368839 2906784 3531190 2706830 9724554 5460432 7705591 5116123 3724145 631161 3432356 7263942 8308052
10 ₁₄₉ 4317021 796354 4233537 8793055 7846210 4747330 3346728 2045020 2162171 2067436 9999997 4416298 1600762 1844082 2610031 5090613 8333172 6573865 5834164 3 6642788 2729440 5784310 1456093 1206945 1607681 8543907 7708940 3364385 3580301 1435518 8541704 5539605	10 ₁₅₀ 8914207 6622548 2806080 2667462 9999997 5802940 1804205 3396611 1922189 5056956 5960179 8422795 5889951 9403167 1577205 3286376 3395558 5644168 1821716 9993287 1938107 8758155 7199889 3807032 1085793 6587160 3395238 4983604 3 2486069	10 ₁₅₁ 9259569 1432043 8011781 6403188 7428871 2406692 4503054 3 6498061 8140093 7846549 7359185 4624762 1987108 1988219 4042865 9999997 5303771 6352289 2017080 2758684 740431 7423981 6607104 8046403 6238269 2051368 1250956 1475800 4635679	10 ₁₅₂ 8250003 1185992 4161550 3125531 4356355 7179596 7417212 4620050 1989996 7010685 7622424 8010004 5863230 3264659 2998692 6098212 9999997 2993963 7089067 4298705 6448452 1749997 6275511 2841987 7967932 4834195 5005300 3272303 3 5046292 4420300 6639870 5165847

10 ₁₅₃	11	10 ₁₅₄	11	10 ₁₅₅	10	10 ₁₅₆	10
9521228	3970116	6027095	317461	3282009	6660103	957621	8540543
478772	1335061	5380202	6047039	3907720	3817807	2117321	2378365
8917003	4564671	1184857	3 6420260	8278671	1218943	4113431	6117190
2257511	7851836	4720309	7586238	5131484	8536081	7640355	9999997
6619192	1077285	4582422	613542	6228192	209896	8988470	2595508
6742841	9999997	1203504	6414574	9999997	7944347	689332	5472441
4652742	3543746	8815143	4232863	5558334	1192453	7820402	3 4349356
791988	6489468	2092409	9178707	6289921	9790104	5796599	8846899
5807012	3 5085796	6508312	2147468	3 4170993	2047102	1818562	690481
3099166	8581089	6947492	9999997	8558224	3377423	9310668	5803632
1682313	575904	3441739	4554082		3052343		4713307
	7051553		1752976				
10 ₁₅₇	10	10 ₁₅₈	10	10 ₁₅₉	10	10 ₁₆₀	10
9088304	5945784	5475661	8457652	913662	3637285	8017892	8758450
911696	6231887	2955202	1284356	9086338	5200983	452736	3413966
3649600	3453741	7897422	3 1061792	3795382	3146505	6462445	9810845
8976111	4078586	7312190	7059086	2262164	9999997	6570835	2995750
4583810	9999997	473335	1886745	6708799	3383682	3 7908884	6029804
7364116	2136005	9143953	4047585	6413356	9282264	4886807	189155
4727853	9155516	2577960	9999997	6555660	1100775	3846996	9390131
5085855	763739	3728446	1123221	4585657	8098016	9999997	2899420
6831355	7398006	6488142	9571521	4614041	3 6209916	4532419	7766649
3336217	3 5321291	9526665	2439905	7924813	7602256	2674307	1938485
			8938208		5512989		8478538
10 ₁₆₁	10	10 ₁₆₂	10	10 ₁₆₃	10	10 ₁₆₄	11
2312614	9600936	3326645	2910636	7268529	6948556	4877615	3 3228708
3161443	2023903	7473833	4115481	2781943	940009	3890518	6595252
7791756	9981623	5476380	9999997	9865974	3166848	4808150	9522183
6613436	728349	1659607	4459856	3330136	8238035	1927693	3685218
6113688	9999997	8340393	5863302	2662508	3 7663412	7889361	9999997
5977723	1561299	4887942	3 4585056	5471771	3841433	1589055	8315075
5683474	8845409	3263166	6138754	5876429	4262154	9321515	5092293
8018931	3 4743066	1806293	4061081	1888703	9999997	1803938	9913535
541831	4637240	6534810	2879745	6565554	3435334	4120905	1265416
9458169	7536620	3254674	8626440	134026	2720553	9348208	7712597
	1998859		5316077		7860847	651792	7599348
							5375341
10 ₁₆₅	10						
2812261	5821472						
8214541	3871331						
3897440	96016						
2106413	7102078						
5405838	221137						
7645550	7375742						
1785459	2863233						
3796699	9999997						
7598074	5029607						
4492663	3 7240983						

Table 2. Minimal stick representatives and candidates. This table contains conformations for the seven knots that we found to have stick numbers lower than their equilateral stick numbers. The first line of each entry indicates the knot type and the provisional stick number, $stick_p(K)$, for that knot. A \star indicates that the value shown is known from theoretical studies to be the actual stick number $stick(K)$.

8 ₁₉	not eq	8 \star	9 ₂₉	not eq	9	10 ₁₆	not eq	11	10 ₇₉	not eq	11
6029799	3 8433120		4772110	1775158	8720545	7217186	3 4760156		4490625	9999997	7408827
6060406	9999997	1573848	5803984	7854373	956331	9025310	1727814	3970782	1911564	3287501	2527736
	3607	3960221	1226643	3621876	6959139	974690	1907658	2188908	2955939	5009687	7402420
9996393	3960220	1567031	8952420	1413283	1287424	8010936	8863748	4470469	5016562	4921563	6412109
3959880	9985379	8454178	1351643	9999997	5035078	3951251	6021718	7224842	4010626	6243749	3099298
3958382	25418	1544761	5921328	4775625	4913828	6597499	1071877	1807033	1119846	3320001	7472264
9987385	6027133	8455239	1047580	3 3885235		8820466	1591721	5625625	8880154	8023123	4736485
	23091	6063673	8428201	7844842	9043669	3061251	5520937	3413751	1133596	9962810	6956014
			1828674	6341874	2009924	5138125	5382031	2402189	5784062	4663750	5085078
						3745626	3655782	8192967	1258440	7042968	3349142
						7449686	9999997	2811251	5312656	3 7140702	

10_{107}	not eq	10	10_{119}	not eq	10	10_{147}	not eq	10
7611873	8435154	3388751	4726094	5242344	2821251	7404452	3	4684297
5616406	3920157	8202186	8290779	4709375	6304374	4363047	8777810	4535860
5850312	3815938	1797814	6274530	2419689	7150467	4258360	4076719	6405390
7874686	5414531	7013280	4679844	6726561	2107970	6131484	3652032	4211797
2433127	4385938	4708594	3940001	6962811	7892030	6343359	4652344	4856641
3589063	6340468	5090000	9554060	4217188	4387188	2595548	1942189	5224140
7877030	3	5785625	445940	5513281	5927187	6445546	9999997	5205547
6212968	9999997	6409062	9176091	9999997	6378749	4393516	3740313	3161954
7032030	4094219	3425626	5626093	3	6290780	5239140	3817344	6838046
2122970	4182657	5488906	4684531	9091404	6792030	3522423	4758906	4168829

DEPARTMENT OF MATHEMATICS/COMPUTER SCIENCE, DUQUESNE UNIVERSITY, PITTSBURGH,
PA 15282, USA

E-mail address: rawd@mathcs.duq.edu

CENTRE FOR EXPERIMENTAL AND CONSTRUCTIVE MATHEMATICS, SIMON FRASER UNIVERSITY,
BURNABY, BC, CANADA

E-mail address: scharein@cecm.sfu.ca